

Minimizing Inventory Costs

Example:

A retail appliance store sells **2500** TV sets per year. It costs **\$10** to store one set for a year. To reorder, there is a fixed cost of **\$20** to cover administrative costs per order, plus **\$9** shipping fee for each set ordered.

a. How many times per year should the store reorder to minimize inventory costs?

Solution:

Let x = number of items per order

$$\begin{aligned} \text{Yearly carrying cost} &= (\text{yearly storage cost per item}) \cdot (\text{average number of items carried}) \\ &= 10 \cdot \frac{x}{2} = 5x \end{aligned}$$

$$\begin{aligned} \text{Yearly reordering cost} &= (\text{cost of each order}) \cdot (\text{number of orders placed per year}) \\ &= (20 + 9x) \cdot \frac{2500}{x} = \frac{50000}{x} + 22500 \end{aligned}$$

$$\begin{aligned} \text{Total Inventory Cost (y)} &= (\text{yearly carrying cost}) + (\text{yearly reordering cost}) \\ y &= (5x) + \left[\frac{50000}{x} + 22500 \right] \end{aligned}$$

$$y' = 5 - \frac{50000}{x^2}$$

$$y' = 0 \text{ when } 5 = \frac{50000}{x^2}$$

$$x^2 = 10000$$

$$x = 100$$

$$y'' = \frac{50000}{x^3} > 0 \text{ when } x = 100, \text{ so the minimum number of orders placed per year} = \frac{2500}{100} = 25 \text{ orders.}$$

b. How many sets should be ordered each time?

Solution:

$x = 100$, so each order should contain 100 TV sets.